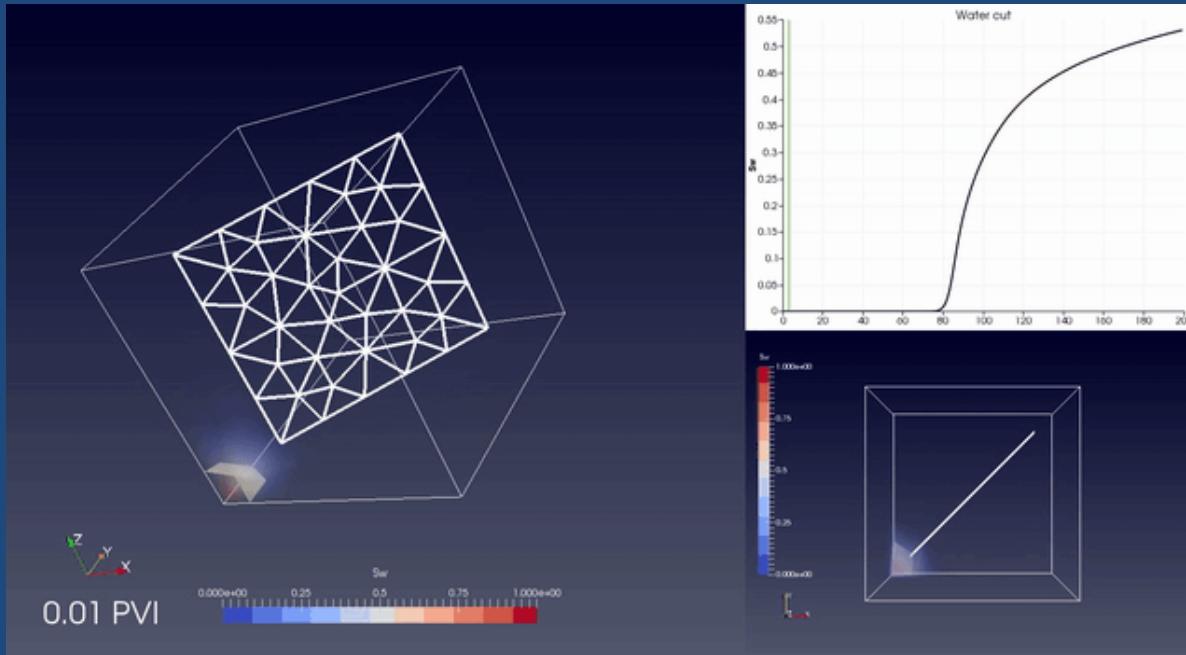


Séminaire du réseau Données et Numérique

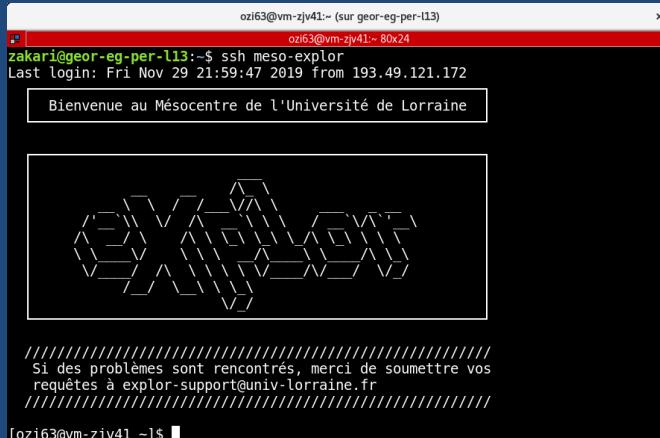


Mustapha Zakari

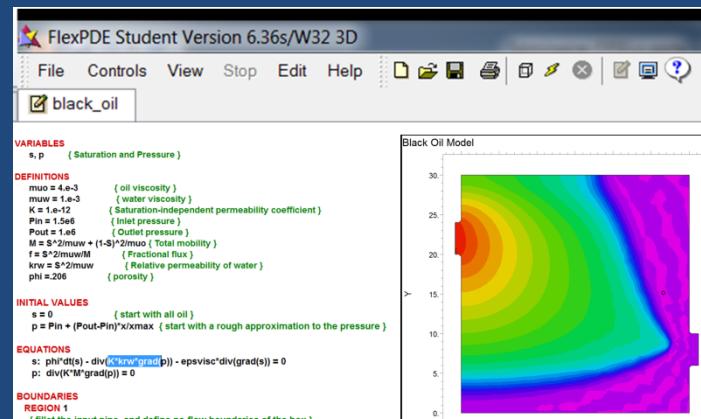
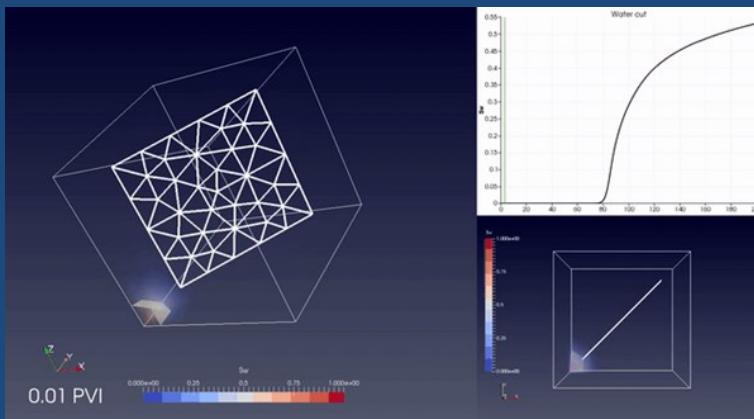
(3/12/2019)

Plan

- EXPLOR – Accélération de codes de calcul



- Modélisation d'écoulements



EXPLOR

Accélération de codes de calcul

- EXPLOR : 6356 coeurs
 - Système d'exploitation : CentOS 7.4
 - Ordonnanceur : SLURM 17.11.3
 - Gestionnaire Environnement : LMOD 7.4
- Parallélisation du calcul approché de π (Fortran 90 +MPI)

EXPLOR – Calcul parallèle de π

Code Fortran + MPI

```
ozi63@vm-zjv41:~/tests/mpif90 (sur geor-eg-per-l13)
ozi63@vm-zjv41:~/tests/mpif90 97x28

program pi
use mpi
implicit none
integer :: code, rang, nbprocs
integer, parameter :: dp = kind(1.d0)
integer, parameter :: li = selected_int_kind(15)
integer(kind=li):: nbblock,i,debut,fin
real(kind=dp) :: largeur,somme,global,x

call MPI_INIT(code)
call MPI_COMM_RANK(MPI_COMM_WORLD,rang,code)
call MPI_COMM_SIZE(MPI_COMM_WORLD,nbprocs,code)
somme = 0._dp
! Nombre d'intervalles
nbblock = 3*1000*1000_li*100
! largeur des intervalles
largeur = 1._dp / real(nbblock,dp)
debut = (rang*nbblock)/nbprocs+1; fin = ((rang+1)*nbblock)/nbprocs
print "(i2,a,1l,a,1l,a,1l)", rang, " debut: ", debut, " fin: ", fin, " delta: ", fin-debut+1
do i=debut, fin
    x = largeur*(i-0.5_dp)
    somme = somme + largeur*(4._dp / (1._dp + x*x))
end do
call MPI_REDUCE(somme, global, 1, MPI_DOUBLE_PRECISION, MPI_SUM, 0, MPI_COMM_WORLD,code)
if (rang ==0) print *, "Pi =", global
call MPI_FINALIZE(code)
end program
```

Méthode des rectangles

$$\pi = \int_0^1 \frac{4}{1+x^2} dx \approx \sum_{i=1}^n \frac{4}{1 + \left(\frac{i - 0.5}{n}\right)^2}$$

EXPLOR – Calcul parallèle de π

Soumission + résultats

Fortran90 + MPI

```
ozi63@vm-zjv41:~/tests/mpif90 (sur geor-eg-per-l13) x
ozi63@vm-zjv41:~/tests/mpif90 88x24
[owi63@vm-zjv41 mpif90]$ sbatch -N 1 -n 2 script2submit.sh
Submitted batch job 161986
[owi63@vm-zjv41 mpif90]$ tail submitted/test_161986.out
 0 debut:          1 fin:    150000000 delta:    150000000
 1 debut:    150000001 fin:    300000000 delta:    150000000
Pi =    3.1415926535893495                                1 nœud, 2 processeurs

real 0m2.845s
user 0m5.110s
sys 0m0.042s
[owi63@vm-zjv41 mpif90]$
[owi63@vm-zjv41 mpif90]$ sbatch -N 1 -n 4 script2submit.sh
Submitted batch job 161987
[owi63@vm-zjv41 mpif90]$ tail submitted/test_161987.out
 0 debut:          1 fin:    75000000 delta:    75000000
 1 debut:    75000001 fin:    150000000 delta:    75000000
 3 debut:   225000001 fin:    300000000 delta:    75000000
 2 debut:   150000001 fin:   225000000 delta:    75000000
Pi =    3.1415926535895338                                1 nœud, 4 processeurs

real 0m1.454s
user 0m5.137s
sys 0m0.067s
[owi63@vm-zjv41 mpif90]$ ■
```

EXPLOR – Exemples d'utilisation

- Le mésocentre : 6356 coeurs
 - Système d'exploitation : CentOS 7.4
 - Ordonnanceur : SLURM 17.11.3
 - Gestionnaire Environnement : LMOD 7.4
- ✓ Parallélisation du calcul approché de π (Fortran 90 +MPI)
 - Code fortran
 - Code MPI
 - Link + compilation : [2procs:2,854s , 4procs:1,454s]
- Peut-on paralléliser des codes Python, Matlab ?
 - Parallélisation (Multithreading) du calcul approché de π :
 - Python + Multiprocessing
 - Matlab + PARallel FOR loops (parfor)

EXPLOR – Calcul parallèle de π

Code Python 3.6 + Multiprocessing

```
ozi63@vm-zjv41:~/tests/python (sur geor-eg-per-l13) x
ozi63@vm-zjv41:~/tests/python 86x26

import multiprocessing as mp
nprocs = mp.cpu_count()
print(f"Number of CPU cores: {nprocs}")

nsteps = 10000000
dx = 1.0 / nsteps
pi = 0.0

def calc_partial_pi(rank, nprocs, nsteps, dx):
    partial_pi = 0.0
    for i in range(rank, nsteps, nprocs):
        x = (i + 0.5) * dx
        partial_pi += 4.0 / (1.0 + x * x)
    partial_pi *= dx
    return partial_pi

inputs = [(rank, nprocs, nsteps, dx) for rank in range(nprocs)]

#Create pool object !STARTS A PARALLEL ZONE!
pool = mp.Pool(processes=nprocs)
result = pool.starmap(calc_partial_pi, inputs)
pi = sum(result)

Méthode des rectangles

$$\pi = \int_0^1 \frac{4}{1+x^2} dx \approx \sum_{i=0}^n \frac{4}{1 + \left(\frac{i + 0.5}{n}\right)^2}$$

```

EXPLOR – Calcul parallèle de π

Résultats

Python + Multiprocessing (Multithreading)

```
ozi63@vm-zjv41:~/tests/python (sur geor-eg-per-l13) x
[ ] ozi63@vm-zjv41:~/tests/python 86x26
Sequential calculation
Sequential version
3.141592653589731
real    0m2.192s
user    0m2.169s
sys     0m0.011s
multiprocessing calculation
Number of CPU cores: 32
3.1415926535897842
real    0m0.228s
user    0m1.323s
sys     0m0.178s
```

1 nœud, 1 cœur

1 nœud, 32 cœurs

EXPLOR – Calcul parallèle de π

Code Matlab + Parfor

Matlab + Parfor

ozi63@vm-zjv41:~/tests/matlab (sur geor-eg-per-l13)

x

ozi63@vm-zjv41:~/tests/matlab 86x28

```
% Parallel Monte Carlo calculation of PI
```

```
parpool('local', str2num(getenv('SLURM_CPUS_ON_NODE')))
```

```
R = 1;
```

```
darts = 1e7;
```

```
count = 0;
```

```
tic
```

```
parfor i = 1:darts
```

```
    % Compute the X and Y coordinates of where the dart hit the
```

```
    % square using Uniform distribution.....
```

```
    x = R*rand(1);
```

```
    y = R*rand(1);
```

```
    if x^2 + y^2 <= R^2
```

```
        % Increment the count of darts that fell inside of the...
```

```
        % circle.....
```

```
        count = count + 1; % Count is a reduction variable.
```

```
    end
```

```
end
```

```
% Compute pi.....
```

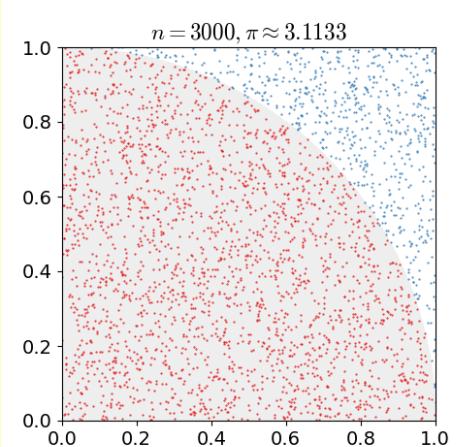
```
myPI = 4*count/darts;
```

```
T = toc;
```

```
fprintf('The computed value of pi is %8.7f.\n', myPI);
```

```
fprintf('The parallel Monte-Carlo method is executed in %8.2f seconds.\n', T);
```

```
delete(gcp);
```



Méthode Monte-Carlo
$$\pi = 4 \frac{counts}{darts}$$

Wikipedia (30 000) darts

EXPLOR – Calcul parallèle de π

Résultats

```
Matlab + Parfor          ozi63@vm-zjv41:~/tests/matlab (sur geor-eg-per-l13) x
ozi63@vm-zjv41:~/tests/matlab 86x28
< M A T L A B (R) >
Copyright 1984-2017 The MathWorks, Inc.
R2017b (9.3.0.713579) 64-bit (glnxa64)
September 14, 2017

connected to 1 workers.                                         1 nœud, 1 cœur

The computed value of pi is 3.1417856.nThe parallel Monte-Carlo method is executed in
14.88 secondsnParallel pool using the 'local' profile is shutting down.
message with properties:

< M A T L A B (R) >
Copyright 1984-2017 The MathWorks, Inc.
R2017b (9.3.0.713579) 64-bit (glnxa64)
September 14, 2017

connected to 32 workers.                                         1 nœud, 32 cœurs

The computed value of pi is 3.1414208.nThe parallel Monte-Carlo method is executed in
0.92 secondsnParallel pool using the 'local' profile is shutting down.
message with properties:
```

EXPLOR – Exemples d'utilisation

Bilan

- ✓ Parallélisation du calcul approché de π (Fortran 90 +MPI)
 - Code fortran
 - Code MPI
 - Link + compilation : [2procs:2,854s ; facteur 1.96 ; 4procs:1,454s]
- ✓ Peut-on paralléliser des codes Python, Matlab ? OUI
 - Parallélisation (Multithreading) du calcul approché de π :
 - ✓ Python + Multiprocessing : [1c:2,192s ; facteur 9.61 ; 32c:0,228s]
 - ✓ Matlab + PARallel FOR loops (parfor) : [1c:14,88s ; facteur 16.2 ; 32c:0,92s]

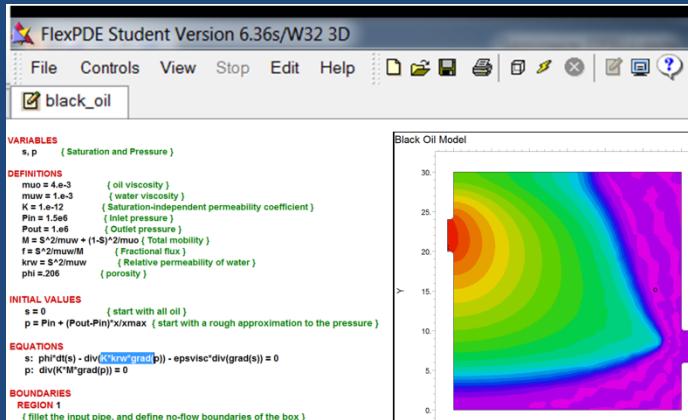
EXPLOR permet d'accélérer des codes Python et/ou Matlab

Plan

- EXPLOR – Exemples d'utilisation

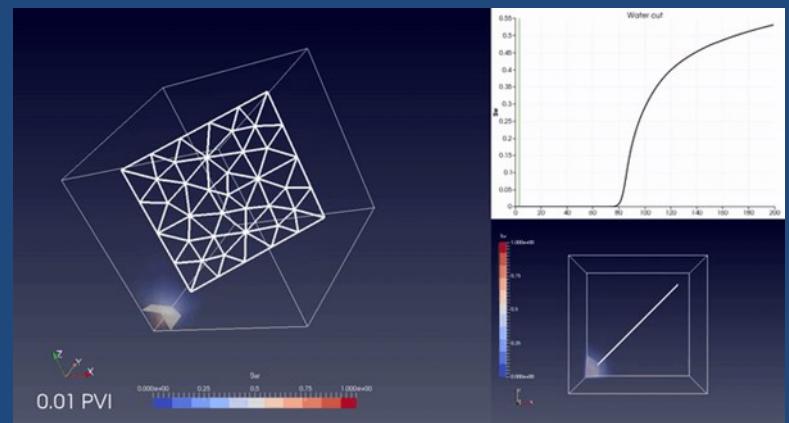
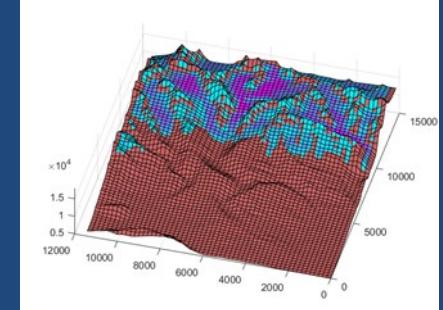


- Modélisation d'écoulements et extrapolations



Modélisation d'écoulements Extrapolations

- Ecoulements glaciaires
 - Equation du modèle
 - Discrétisation
 - Premiers Résultats
- Ecoulements diphasiques en milieux poreux fracturés
 - Equations du modèle
 - Discrétisation
 - Premiers Résultats



Ecoulements glaciaires

- **Equation du modèle :** Shallow Ice Approximation [Hutter 1983]
 - Loi de conservation + loi visqueuse de Glen

$$\left\{ \begin{array}{lcl} \frac{\partial H}{\partial t} - \nabla \cdot \mathbf{q} & = & a \\ \mathbf{q} & = & D \nabla s \\ D & = & C H^{n+2} |\nabla s|^{n-1} \\ s & = & b + H \end{array} \right.$$

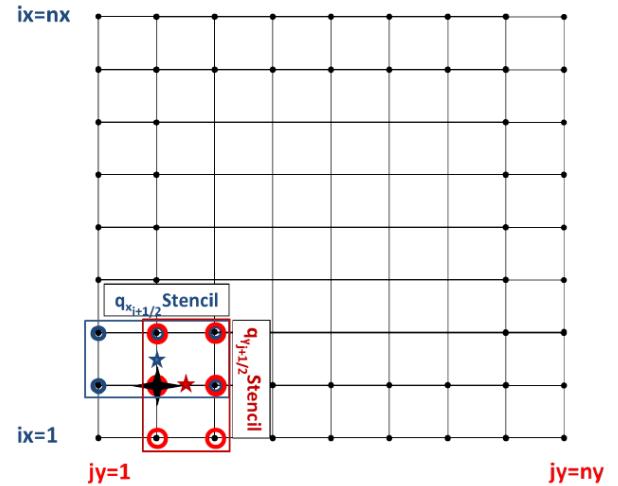
- Avec :
 - H l'épaisseur de glace
 - b et s le bedrock et la hauteur totale
 - a le terme d'accumulation/ablation
 - q le flux de glace et D le coefficient de diffusion
 - C une constante fixant la loi d'écoulement

Ecoulements glaciaires

– Discrétisation : Differences Finies + Explicite [Hindmarsh, 1996]

$$\left\{ \begin{array}{lcl} \frac{\partial H}{\partial t} - \nabla \cdot \mathbf{q} & = & a \\ \mathbf{q} & = & D \nabla s \\ D & = & C H^{n+2} |\nabla s|^{n-1} \\ s & = & b + H \end{array} \right.$$

$$H_{i,j}^{k+1} = H_{i,j}^k + \frac{\Delta t}{\Delta x} \left(q_{x_{i+\frac{1}{2}}}^k - q_{x_{i-\frac{1}{2}}}^k + q_{y_{j+\frac{1}{2}}}^k - q_{y_{j-\frac{1}{2}}}^k \right) + \Delta t \times a_{i,j}^k$$

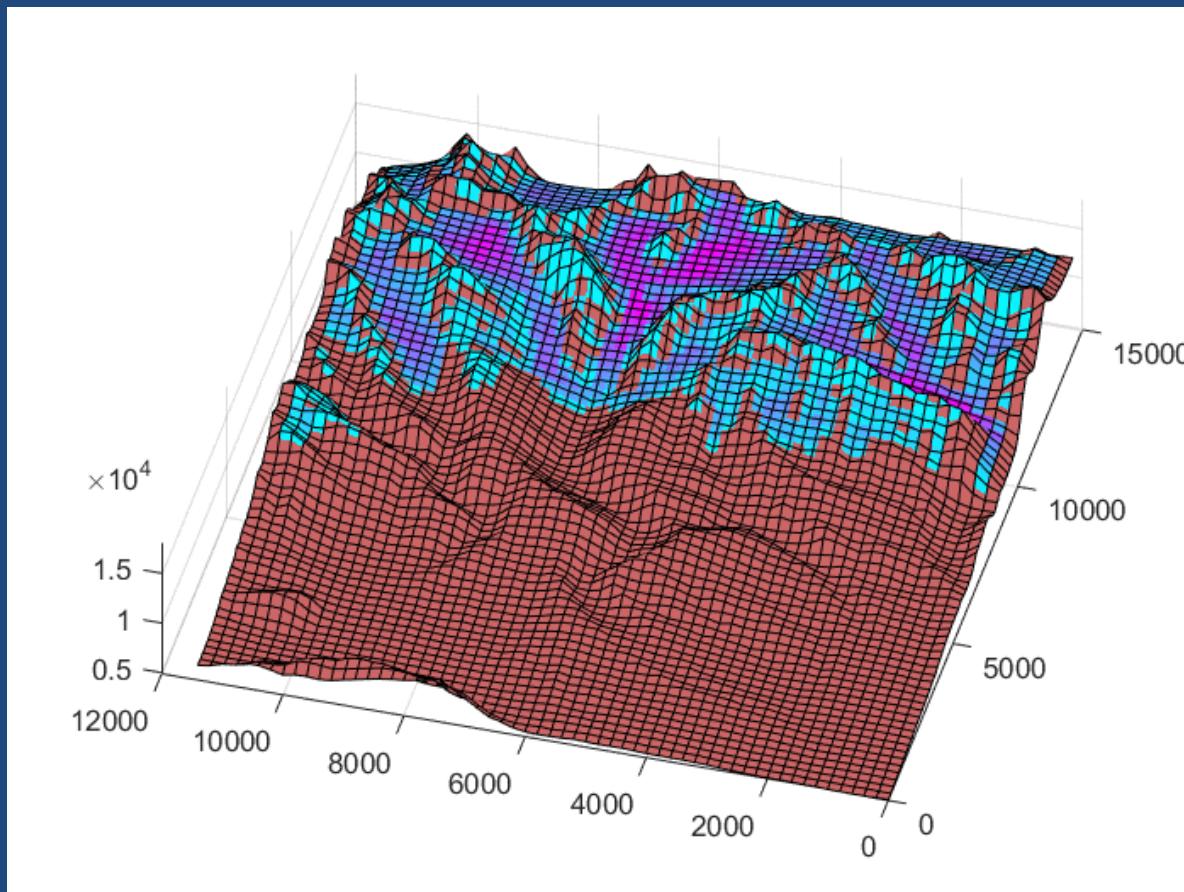


$$\left\{ \begin{array}{lcl} q_{x_{i+\frac{1}{2}}} & = & C_{i,j} \left[\frac{H_i + H_{i+1}}{2} \right]^5 \left(\left(\frac{H_{i+1} - H_i}{\Delta x} \right)^2 + \left(\frac{H_{i,j+1} - H_{i,j-1} + H_{i+1,j+1} - H_{i+1,j-1}}{4\Delta y} \right)^2 \right) \left(\frac{H_{i+1} - H_i}{\Delta x} \right) \\ q_{x_{i-\frac{1}{2}}} & = & C_{i,j} \left[\frac{H_{i-1} + H_i}{2} \right]^5 \left(\left(\frac{H_i - H_{i-1}}{\Delta x} \right)^2 + \left(\frac{H_{i-1,j+1} - H_{i-1,j-1} + H_{i,j+1} - H_{i,j-1}}{4\Delta y} \right)^2 \right) \left(\frac{H_i - H_{i-1}}{\Delta x} \right) \end{array} \right.$$

$$\left\{ \begin{array}{lcl} q_{y_{j+\frac{1}{2}}} & = & C_{i,j} \left[\frac{H_j + H_{j+1}}{2} \right]^5 \left(\left(\frac{H_{j+1} - H_j}{\Delta y} \right)^2 + \left(\frac{H_{i+1,j} - H_{i-1,j} + H_{i+1,j+1} - H_{i-1,j+1}}{4\Delta x} \right)^2 \right) \left(\frac{H_{j+1} - H_j}{\Delta y} \right) \\ q_{y_{j-\frac{1}{2}}} & = & C_{i,j} \left[\frac{H_{j-1} + H_j}{2} \right]^5 \left(\left(\frac{H_j - H_{j-1}}{\Delta y} \right)^2 + \left(\frac{H_{i+1,j-1} - H_{i-1,j-1} + H_{i+1,j} - H_{i-1,j}}{4\Delta x} \right)^2 \right) \left(\frac{H_j - H_{j-1}}{\Delta y} \right) \end{array} \right.$$

Modélisation d'écoulements glaciaires

– Simulation Matlab



Hauteur de glace sur 1000 ans, : [Lavé,Zakari CRPG]

Ecoulements diphasiques en milieux poreux fracturés

– Equations du modèle : Darcy + lois de conservations

- Pression:

$$\nabla \cdot (-\lambda_T \nabla P) = \frac{q_w}{\rho_w} + \frac{q_o}{\rho_o} \quad \lambda_T = \lambda_w + \lambda_o$$

- Saturation en eau

$$\Phi \frac{\partial S_w}{\partial t} + \nabla \cdot \left(\frac{\lambda_w}{\lambda_T} \nabla P \right) = \frac{q_w}{\rho_w}$$

– Avec :

- w l'eau et o l'huile
- S_w la saturation en eau
- Φ La porosité
- P la pression
- λ_T la mobilité totale
- ρ la masse volumique
- q les termes d'injection/aspiration

Ecoulements diphasiques en milieux poreux fracturés

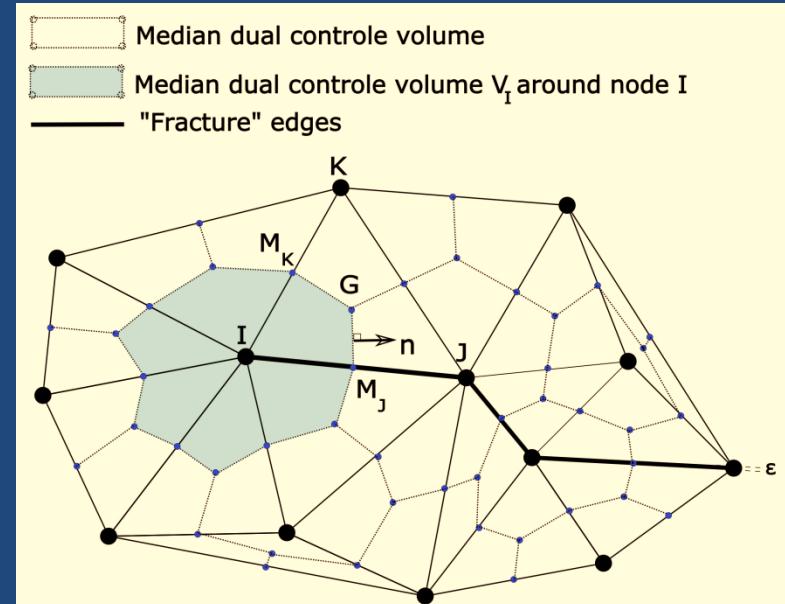
– Discrétisation : **Volumes-Finis** centrés aux nœuds, Explicite en

$$\begin{aligned} & \sum_{IJK \in \Omega_m} \left[-|M_J G| \lambda_T(S_{w,M_J G}) \sum_{j=1}^3 P_j \nabla \Phi_j \cdot \mathbf{n}_{M_J G} - |M_K G| \lambda_T(S_{w,M_K G}) \sum_{j=1}^3 P_j \nabla \Phi_j \cdot \mathbf{n}_{M_K G} \right] \\ & + \sum_{IJ \in \Omega_f} \left[-0.5\varepsilon (\lambda_T(S_{w,J}) - \lambda_T(S_{w,I})) \frac{P_J - P_I}{IJ} \right] = q_I A_I \end{aligned}$$

$$\nabla \cdot (-\lambda_T \nabla P) = \frac{q_w}{\rho_w} + \frac{q_o}{\rho_o} \quad \lambda_T = \lambda_w + \lambda_o$$

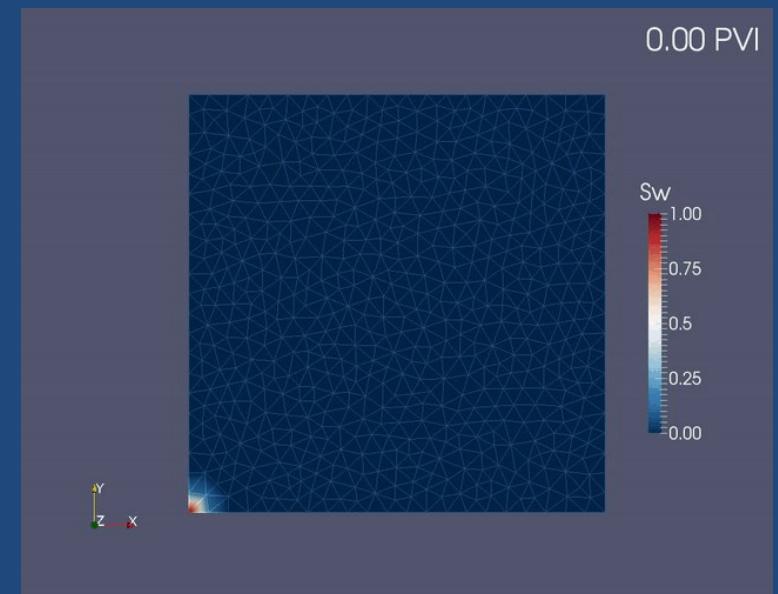
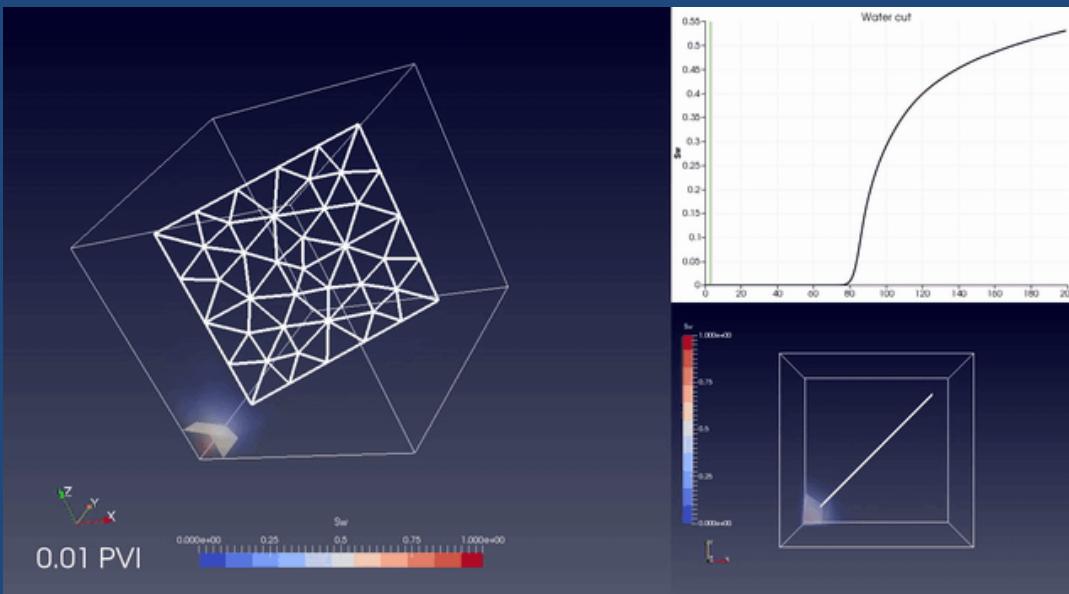
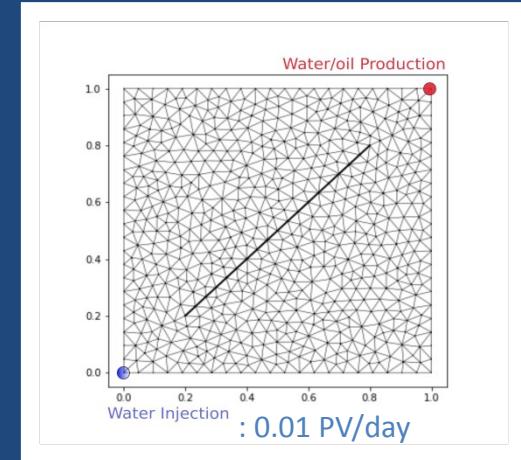
$$\begin{aligned} S_{w,I}^{t+\Delta t} &= S_{w,I}^t \\ &+ \frac{\Delta t}{A_{por,I}} \sum_{IJK \in \Omega_m} \left[f_w(S_{w,M_J G}^{up}) |M_J G| \lambda_T(S_{w,M_J G}) \sum_{j=1}^3 P_j \nabla \Phi_j \cdot \mathbf{n}_{M_J G} \right] \\ &+ \frac{\Delta t}{A_{por,I}} \sum_{IJK \in \Omega_m} \left[f_w(S_{w,M_K G}^{up}) |M_K G| \lambda_T(S_{w,M_K G}) \sum_{j=1}^3 P_j \nabla \Phi_j \cdot \mathbf{n}_{M_K G} \right] \\ &+ \frac{\Delta t}{A_{por,I}} \sum_{IJ \in \Omega_f} \left[0.5\varepsilon f_w(S_{w,IJ}^{up}) (\lambda_T(S_{w,J}) - \lambda_T(S_{w,I})) \frac{P_J - P_I}{IJ} \right] \\ &+ \frac{\Delta t}{A_{por,I}} (max(q_I, 0) + f_w min(q_I, 0)) A_I \end{aligned}$$

$$\Phi \frac{\partial S_w}{\partial t} + \nabla \cdot \left(\frac{\lambda_w}{\lambda_T} \nabla P \right) = \frac{q_w}{\rho_w}$$



Ecoulements diphasiques en milieux poreux fracturés

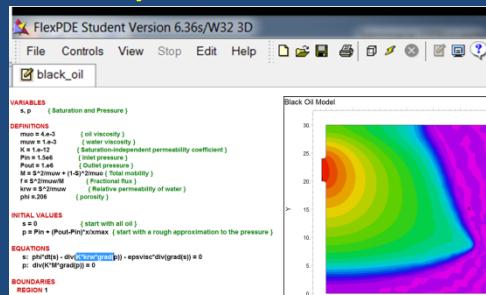
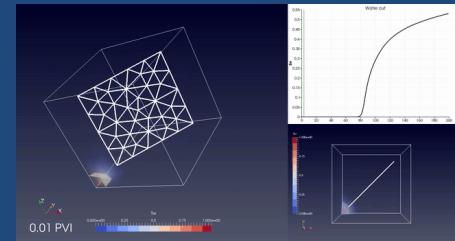
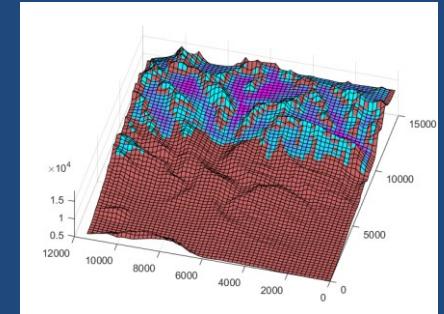
– Résultats 2D et 3D : Saturation en eau



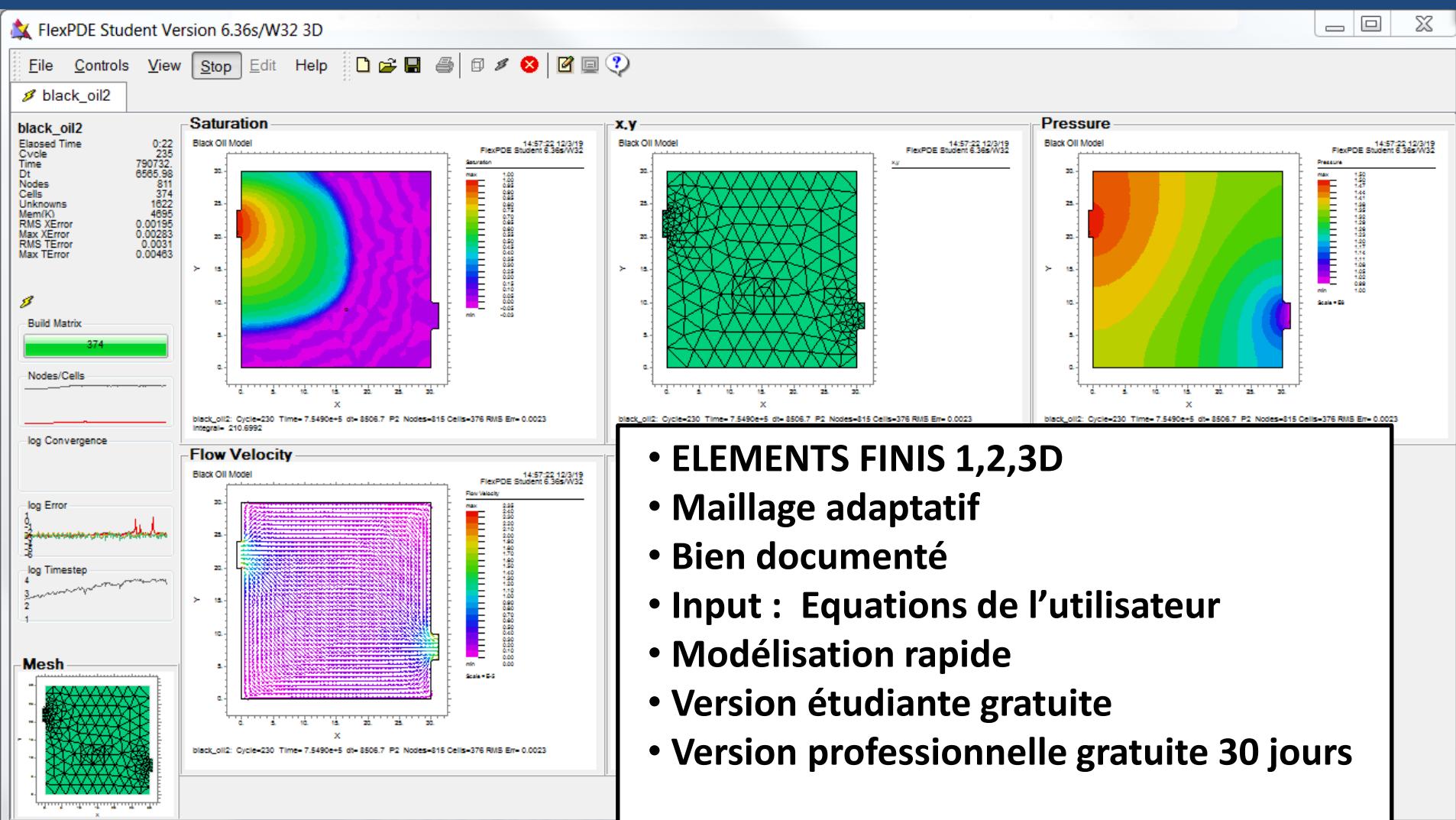
Modélisation d'écoulements

Extrapolations

- Ecoulements glaciaires
 - Equation du modèle
 - Discrétisation
 - Premiers Résultats
- Ecoulements diphasiques en milieux poreux fracturés
 - Equations du modèle
 - Discrétisation
 - Premiers Résultats
- Connaissant les équations d'un modèle peut-on ?
 - Eviter de discréteriser ?
 - Eviter de tout coder ?
 - Ecoulements avec FlexPDE



FlexPDE



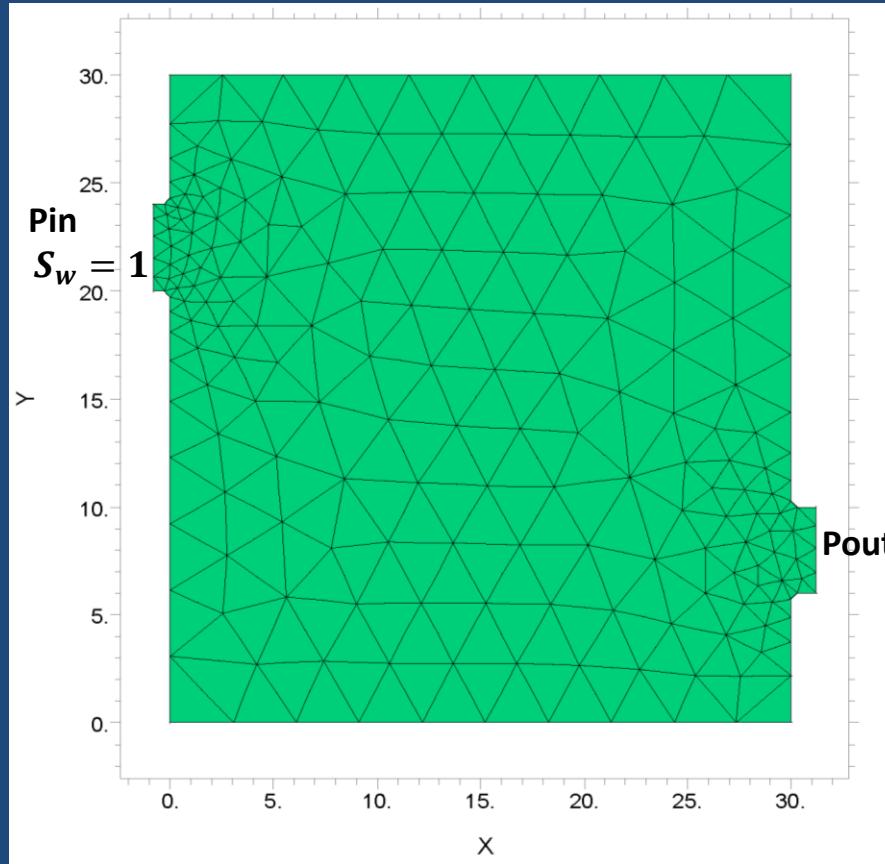
- ELEMENTS FINIS 1,2,3D
- Maillage adaptatif
- Bien documenté
- Input : Equations de l'utilisateur
- Modélisation rapide
- Version étudiante gratuite
- Version professionnelle gratuite 30 jours

Ecoulements avec FlexPDE

Exemple : Black Oil - Equations

$$\Phi \frac{\partial S_w}{\partial t} + \nabla \cdot \left(\frac{\lambda_w}{\lambda_T} \nabla P \right) = 0$$

$$\nabla \cdot (-\lambda_T \nabla P) = 0 \quad \lambda_T = K k r_w$$



Ecoulements avec FlexPDE

Exemple : Black Oil – Script FlexPDE1

$$\Phi \frac{\partial S_w}{\partial t} + \nabla \cdot \left(\frac{\lambda_w}{\lambda_T} \nabla P \right) = 0$$

$$\nabla \cdot (-\lambda_T \nabla P) = 0 \quad \lambda_T = K k r_w$$

TITLE 'Black Oil Model'

VARIABLES

s, p {Saturation and Pressure}

DEFINITIONS

Pin = 1.5e6	{ Inlet pressure }
Pout = 1.e6	{ Outlet pressure }
phi = .206	{ porosity }
K = 1.e-12	{ Saturation-independent permeability coefficient }
krw = S^2/muw	{ Relative permeability of water }
epsvisc = 1.e-6	{ A little artificial diffusion to smooth the solution }
sint = integral(s)	{ the total extraction integral }

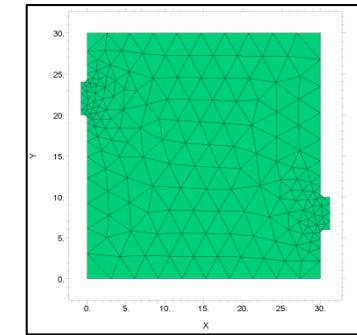
...

INITIAL VALUES

s = 0	{ start with all oil }
p = Pin + (Pout-Pin)*x/xmax	{ Initial Pressure approximation}

EQUATIONS

s: phi*dt(s) - div(K*krw*grad(p)) - epsvisc*div(grad(s)) = 0
p: div(K*M*grad(p)) = 0



Ecoulements avec FlexPDE

Exemple : Black Oil – Script FlexPDE2

BOUNDARIES

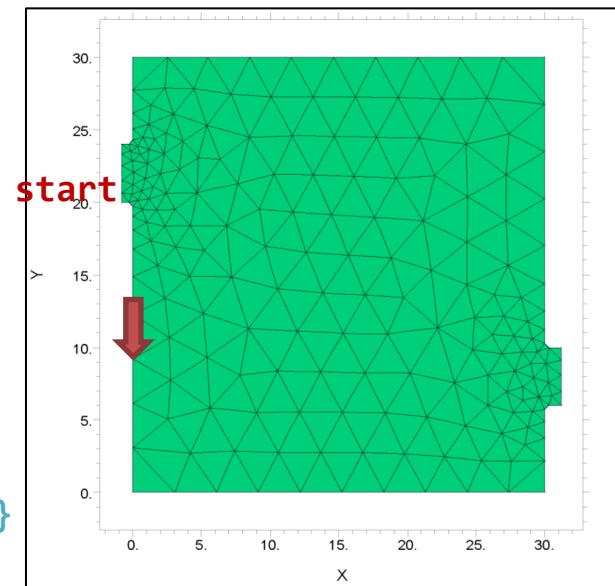
REGION 1

```
{ fillet the input pipe, and define no-flow boundaries of the box }
start(-2*rad,in_ctr-diam)
natural(p)=0 natural(s) = 0
line to (0,in_ctr-diam) bevel(rad)
line to (0,0) to (xmax,0) to (xmax,out_ctr-diam) bevel(rad)
line to (xmax+3*rad,out_ctr-diam)

{ set constant outlet pressure, and "tautological" saturation flux }
value(p) = Pout
natural(s) = -K*krw*dx(p)
line to (xmax+3*rad,out_ctr+diam)

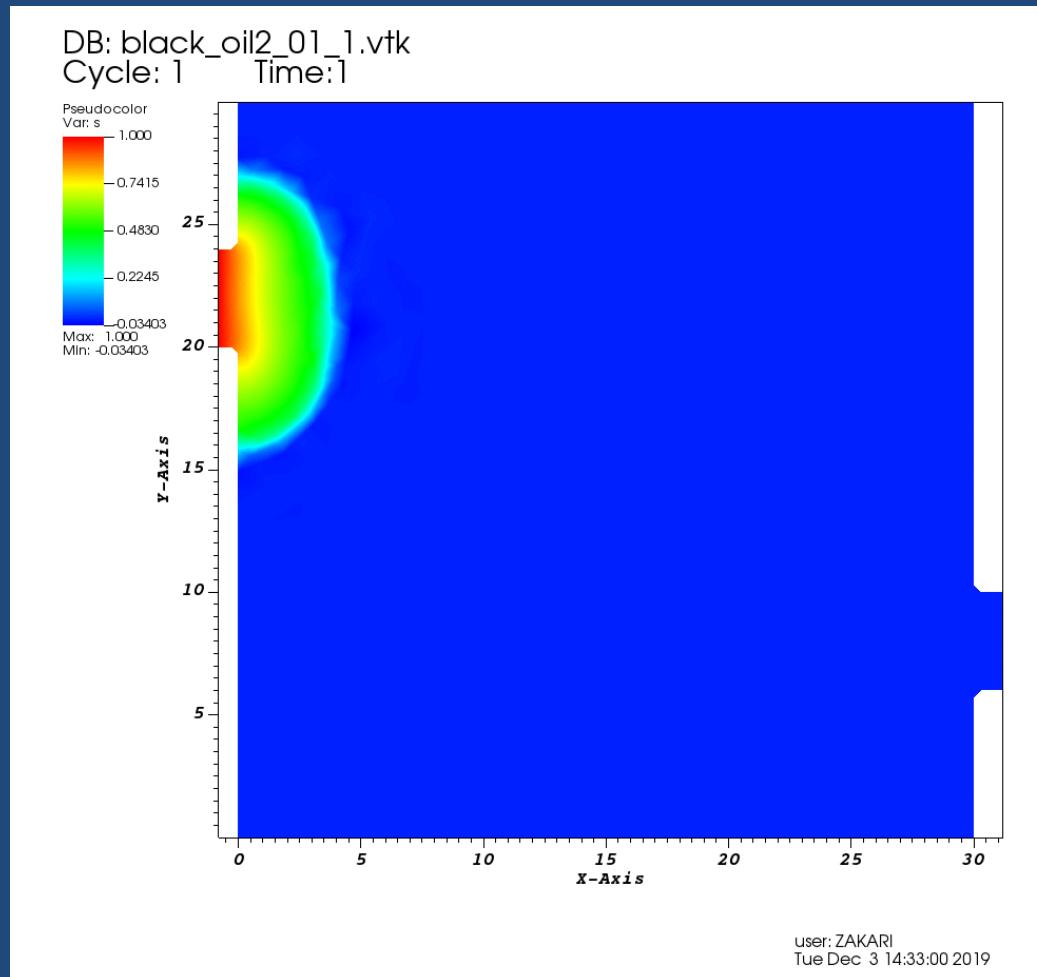
{ reset no-flow box boundaries }
natural(p)=0 natural(s)=0
line to (xmax,out_ctr+diam) bevel(rad)
line to (xmax,ymax) to (0,ymax)
    to (0,in_ctr+diam) bevel(rad)
line to (-2*rad,in_ctr+diam)

{ set constant inlet pressure and saturation }
value(p) = Pin    value(s) = 1
line to close
```



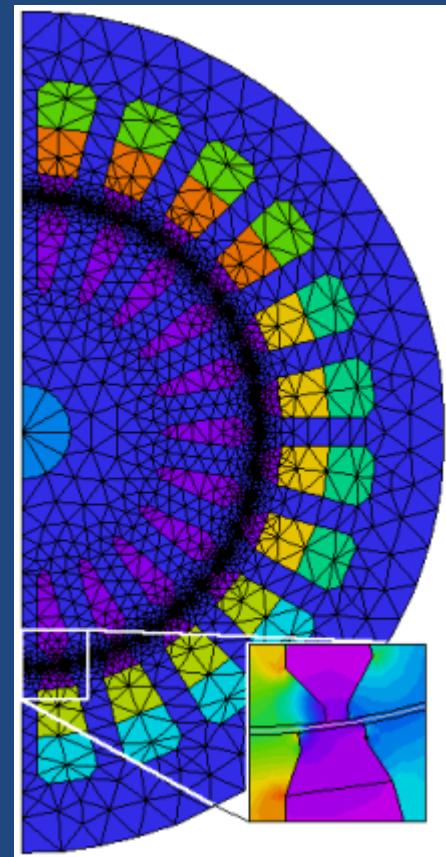
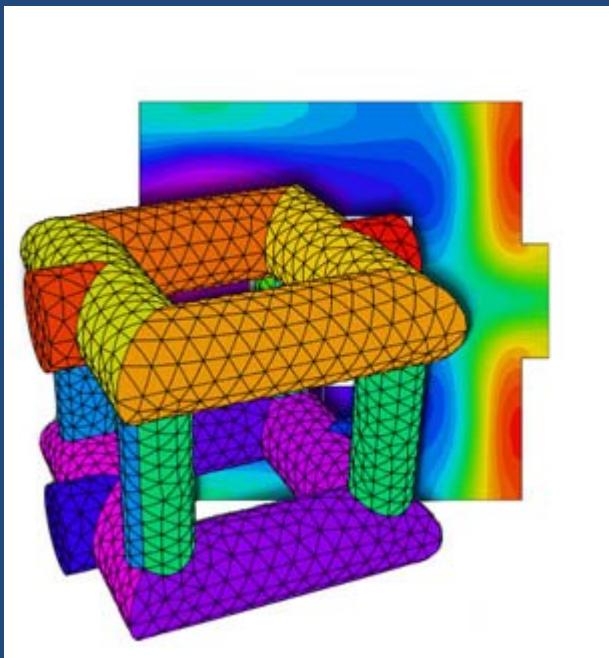
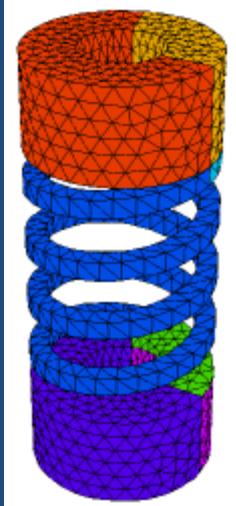
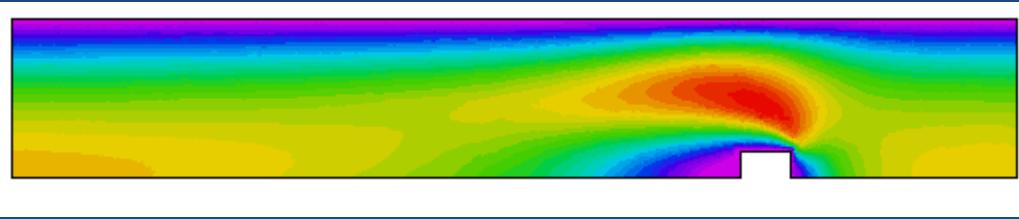
Ecoulements avec FlexPDE

Exemple : Black Oil - Résultats



Saturation en eau

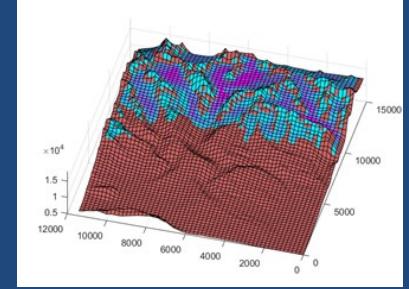
Autres modélisations FlexPDE



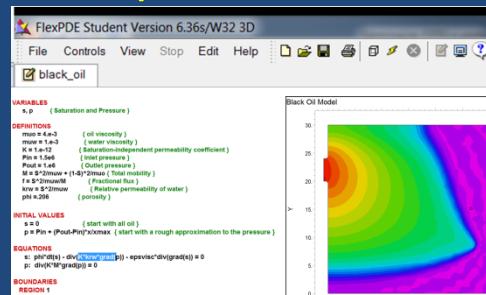
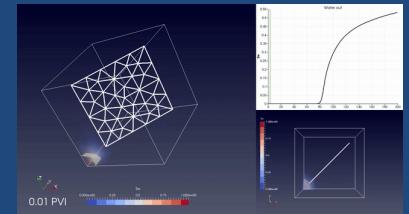
Modélisation d'écoulements

Extrapolations

- Ecoulements glaciaires
 - Equation du modèle
 - Discrétisation
 - Premiers Résultats



- Ecoulements diphasiques en milieux poreux fracturés
 - Equations du modèle
 - Discrétisation
 - Premiers Résultats
- Connaissant les équations d'un modèle peut-on ? OUI
 - ✓ Eviter de discréteriser ?
 - ✓ Eviter de tout coder ?
 - ✓ Ecoulements avec FlexPDE



Conclusion

- Calcul parallèle possible en python (**Multiprocessing**)
- Calcul parallèle possible en Matlab (**Parfor**)
- Modélisations Eléments-Finis réalisables avec **FlexPDE**
 - Sans discréteriser
 - Sans vraiment coder

Merci pour votre attention